

Math 486: Game Theory
Assignment 12
Due Mon Dec 3

The topics for this assignment are discussed in Binmore Chapter 8. Binmore is on 2 hour reserve in the math library on the ground floor of McAllister.

1. The payoff bimatrix for the Prisoner's Dilemma is

	<i>Dove</i>	<i>Hawk</i>
<i>Dove</i>	(3,3)	(0,6)
<i>Hawk</i>	(6,0)	(1,1)

Show that (**Hawk,Hawk**) is the unique Nash equilibrium for a finite stage game whose stage game is the Prisoner's Dilemmas, where **Hawk** is the strategy that plays *Hawk* in every stage.

2. For an iterated game whose stage game is the Prisoner's Dilemma, the **Grim** strategy is to play *Dove* in the first stage, and to continue to play *Dove* unless the other player plays *Hawk*, in which case, play *Hawk* for the rest of the game.

Let G be the indefinite stage game whose stage game is the Prisoner's Dilemma and where, after each stage is played, the probability of playing another stage is p . What is the smallest value of p making (**Grim,Grim**) a Nash equilibrium?

3. Let G be the infinite stage game whose stage game is the Prisoner's Dilemma. Draw diagrams for a pair of finite state automatons, **Puff Daddy** and **P. Diddy**, that play the game G , such that
 - (a) The long run average payoff vector when **Puff Daddy** plays **P. Diddy** is (4, 2).
 - (b) The pair of strategies (**Puff Daddy,P. Diddy**) is a Nash equilibrium.

Explain why your finite state automatons satisfy the requirements (a) and (b).